Problems 1 and 2 use the concept of “electronegativity” to analyze the strength of a polar AB bond and to contrast the π-bonding ability of C and Si. “Electronegativity” is closely related to the ionization energy of an atomic orbital, and it is expressed in units of eV. You will need to use non-degenerate perturbation theory to answer these questions.

1. In this problem we want to approximate the strength of a two electron bond between two atoms (A and B) with different electronegativities. Approximate the molecular orbitals as linear combinations of one valence orbital on A and another on B

\[ \psi \equiv c_1 \phi_A + c_2 \phi_B \]

For simplicity, assume that the atomic orbitals are approximately orthogonal

\[ S \equiv \int \phi_A \phi_B \, d\tau \approx 0. \]

A. We now want to approximate the energy of the AB bond for a fixed atom A bonding to different partners B with varying electronegativity. To this end, fix the electronegativity of atom A (\( \varepsilon_A \)) and allow the electronegativity of B (\( \varepsilon_B \)) to vary freely. Finally, assume the coupling matrix element is independent of the electronegativity and (arbitrarily) equal to 1

\[ V \equiv \int \phi_A \hat{H} \phi_B \, d\tau \approx 1. \]

Within this model, compute the binding energy of the lowest MO as a function of \( \varepsilon_B \). That is to say, compute the difference in energy between the lowest MO and the lowest AO as you vary the electronegativity of atom B. What electronegativity produces the strongest AB bond? Does this agree with your chemical intuition? You may wish to look up a few A-B bond strengths to substantiate your argument.

B. The model above is missing electron-electron interactions. *Qualitatively* speaking, how would you expect the results of part A to change if you included electron-electron interactions at the level of the Independent Electron Approximation (IEA)? Be as specific as you can in your answer. For example, will the bond get stronger or weaker? Will the optimal electronegativity change?
2. Unsaturation (i.e. the existence of stable multiple bonds) is an extremely important phenomenon for the chemistry of carbon. However, it is comparatively rare for silicon even though C and Si have the same valence shell. In this problem, we develop an explanation for this based on MO theory. Consider the ethylene molecule (H₂C=CH₂) oriented in the x-y plane. At equilibrium, the MO Hamiltonian for the carbon pₓ orbitals is

\[ H_{C-C} = \begin{pmatrix} -10.9 & -0.8 \\ -0.8 & -10.9 \end{pmatrix} \]

Answer the following questions. In preparing your answer it may prove useful to know the following data:

<table>
<thead>
<tr>
<th></th>
<th>Silicon</th>
<th>Carbon</th>
</tr>
</thead>
<tbody>
<tr>
<td>Electronegativity</td>
<td>1.90eV</td>
<td>2.55eV</td>
</tr>
<tr>
<td>Atomic Radius</td>
<td>1.46 Å</td>
<td>0.91 Å</td>
</tr>
</tbody>
</table>

A. Consider the two molecules H₂Si=SiH₂ and H₂Si=CH₂ at their respective equilibrium geometries. Of the eight matrices below, one represents the Hamiltonian for the pₓ orbitals in H₂Si=SiH₂, while another represents H₂Si=CH₂. Which is which? Justify your answer.

\[
\begin{pmatrix} -8.9 & -1.0 \\ -1.0 & -8.9 \end{pmatrix}, \begin{pmatrix} -8.9 & -0.4 \\ -0.4 & -8.9 \end{pmatrix}, \begin{pmatrix} -12.3 & -0.4 \\ -0.4 & -12.3 \end{pmatrix}, \begin{pmatrix} -12.3 & -1.0 \\ -1.0 & -12.3 \end{pmatrix}, \begin{pmatrix} -8.9 & -0.6 \\ -0.6 & -8.9 \end{pmatrix}, \begin{pmatrix} -12.3 & -0.9 \\ -0.9 & -12.3 \end{pmatrix}, \begin{pmatrix} -8.9 & -10.9 \\ -10.9 & -8.9 \end{pmatrix}, \begin{pmatrix} -12.3 & -10.9 \\ -10.9 & -12.3 \end{pmatrix}
\]

B. Based on your answer to part A, how do you expect the strength of the π bonds in H₂Si=SiH₂ and H₂Si=CH₂ to compare to the strength of the π bond in ethylene? Justify your answer.

**Special Note:** Problems 3-6 deal with the computer calculations based on Professor Van Voorhis’ two Lectures (28 and 29, given November 20 and 27). Several of these problems require Gaussian calculations, which produce a “.log” file detailing the results of the calculation. In order to receive full credit for this problem set, you must submit the “.log” files for your calculations electronically via the 5.61 website. While we encourage you to work together on these problems, each student is expected to run their own calculations.

3. In this problem we’re going to familiarize ourselves with using Gaussian by finding the equilibrium structure of a single methanol molecule.

A. Make a reasonable guess at the structure of CH₃OH using GaussView. Then, determine the equilibrium structure of the molecule in the Hartree-Fock (HF) approximation using the 6-31G(d,p) basis. What are the
predicted equilibrium bond lengths, bond angle and dipole moment of the molecule? Compare your results with the experimental values of $R_{\text{OH}}=0.956$ Å, $R_{\text{CO}}=1.427$ Å, $R_{\text{CH}}=1.096$ Å, $R_{\text{OCH}}=1.096$ Å, $\theta_{\text{HCH}}=109.0^\circ$, $\theta_{\text{HOC}}=108.9^\circ$ and $\mu=1.70$ Debye, respectively.

**B.** Use GaussView to visualize the molecular orbitals. What are the HOMO and LUMO? Are they bonding? Antibonding? $\sigma$ or $\pi$? Lone pair orbitals? What does this tell you about where the electron would come from if you ionized formaldehyde to make $\text{H}_2\text{CO}^+$?

4. Methanol combustion in the gas phase follows the reaction:

$$\text{CH}_3\text{OH}(g) + \frac{3}{2} \text{O}_2(g) \rightarrow \text{CO}_2(g) + 2\text{H}_2\text{O}(g) \quad \Delta E=???$$

This reaction is extremely exothermic and makes methanol, which is a very efficient fuel. In this problem, we will use various methods to approximate the energy released by this reaction.

$$\Delta E=E(\text{CH}_3\text{OH}) + \frac{3}{2} E(\text{O}_2) - E(\text{CO}_2) - 2 E(\text{H}_2\text{O})$$

**A.** First, let’s try using the HF/6-31G(d,p) approximation that worked so well for the structure of methanol above. Obtain HF/6-31G(d,p) optimized structures for the reactants and both products. Each of these calculations should be strictly analogous to the calculation you did in the previous problem. Compare your bond lengths to the experimental values. For $\text{O}_2$ $R_{\text{OO}}=1.208$ Å; for $\text{CO}_2$ $R_{\text{CO}}=1.162$ Å; and for water $R_{\text{OH}}=.958$ Å, $\theta=104.5^\circ$.

**B.** Use the final energies of $\text{CH}_3\text{OH}$, $\text{O}_2$, $\text{CO}_2$, and $\text{H}_2\text{O}$ to compute the energy released in burning one molecule of methanol. Compare your prediction to the experimental result $\Delta E=-7.1$ eV. Note that your answer will not be very close. Does this surprise you? Why or why not?

**C.** The discrepancy above must come from one of two sources: either the basis set is not big enough, or the Hartree-Fock energy expression is not accurate enough. First, let us see if the basis set is the problem. Choose a larger basis set than 6-31G(d,p) for this system and justify why you chose this basis. Now, compute the reaction energy in this basis. Does a larger basis significantly change your answer? [Note: If you chose an extremely large basis, this calculation could take quite some time.]

**D.** Next, let’s see if a better energy function can improve matters. Use density functional theory (DFT) to compute the reaction energy. Does DFT bring your answer into closer agreement with experiment? What do you take home from this exercise? [Note: in this part, you may use an energy functional and basis set of your choice, but you must justify your choice.]
5. One of the most important intermolecular interactions in chemistry is the hydrogen bond. In particular, hydrogen bonding in water is an extremely important topic. In this problem, we will study the hydrogen bond between two water molecules.

A. Compute the length, $R$, of a hydrogen bond between two water molecules using B3LYP in a 6-31G(d,p) basis. To do this, you will need to optimize the geometry of a pair of water molecules placed close to one another:

![Diagram of a hydrogen bond between two water molecules]

How does the length of the H--O hydrogen bond compare to the O-H bond in water?

B. Now, compute the binding energy of the hydrogen bond using B3LYP/6-31G(d,p):

$$\Delta E = E(2 \text{ H}_2\text{O}) - 2 \cdot E(\text{H}_2\text{O})$$

How does the strength of the hydrogen bond compare to the strength of an OH-bond in water?

C. Redo your calculations from part B using MP2. Do the density functional results agree with the correlated calculations as far as the strength of the hydrogen bond goes? [Note: you will need to justify your choice of basis set for this part of the problem.]

D. Now, consider a model where the interaction between two water molecules (A and B) is entirely due to their dipole moments ($\mu_A$ and $\mu_B$). The most favorable configuration would then place the two dipole moments head-to-tail (i.e. $\rightarrow \cdots \rightarrow$) in which case the interaction energy is given by

$$\Delta E = -2 \frac{\mu_A \mu_B}{R_{AB}^3}$$

Compute the maximum binding energy of the water dimer within this dipole-dipole model [Hint: You will need to compute the dipole moment of a single water molecule first]. Does the dipole model agree qualitatively with the computed orientations of the two molecules in the water dimer? Does it accurately predict the binding energy? Explain any discrepancies you find.
E. Now, compute the binding energy of H₂S dimer. How much weaker is the bond between two H₂S molecules, as compared to two water molecules? How close is the energy of (H₂S)₂ to the energy predicted by the dipole-dipole model?

F. Do your results in parts D and E support the existence of a “hydrogen bond” between two water molecules?

6. Answer one of the following questions using Gaussian calculations. Describe what calculations you performed to obtain your answer and why. Do your answers agree with your chemical intuition? You may use any method/basis combination you wish, but please explain your choice. For extra credit, you may perform multiple portions of this problem.

A. What is the energy gain on forming the peptide bond in (Ala)₂?

$$\text{Ala-OH} + H\text{-Ala} \rightarrow \text{Ala}_2 + H_2O$$

Compare this to the energy gained from the peptide bond between Alanine and Valine:

$$\text{Ala-OH} + H\text{-Val} \rightarrow \text{Ala-Val} + H_2O$$

B. What is the length of the carbon-carbon bond in C₆₀? Compare this to the bond length in benzene. What does this say about the C-C bond order in C₆₀?

C. What is the energy difference between the high and low spin states of Fe(2-picolyamine)₃, shown below?

![Chemical structure](image)

D. What is the ionization potential of Ferrocene, Fe(C₅H₅)₂? Where does the ionized electron come from (metal or ligand)? How does the IP compare to the IP for, say, water?

E. Pick a chemical question of interest to you and answer it with a calculation.