

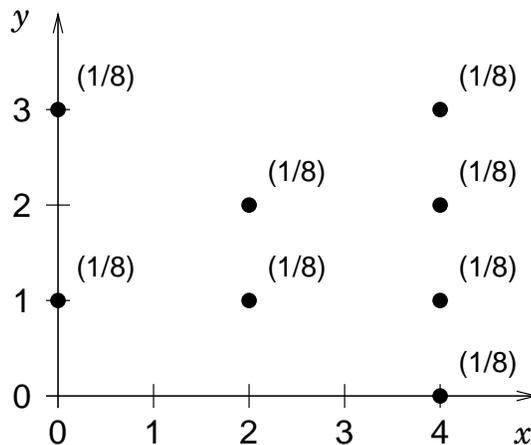
Recitation 6
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1. Consider an experiment in which a fair four-sided die (with faces labeled 0, 1, 2, 3) is thrown once to determine how many times a fair coin is to be flipped. In the sample space of this experiment, random variables N and K are defined by

- N = the result of the die roll
- K = the total number of heads resulting from the coin flips

- (a) Determine and sketch $p_N(n)$
- (b) Determine and tabulate $p_{N,K}(n, k)$
- (c) Determine and sketch $p_{K|N}(k | 2)$
- (d) Determine and sketch $p_{N|K}(n | 2)$

2. Consider an outcome space comprising eight equally likely event points, as shown below:



- (a) Which value(s) of x maximize(s) $\mathbf{E}[Y | X = x]$?
- (b) Which value(s) of y maximize(s) $\text{var}(X | Y = y)$?
- (c) Let $R = \min(X, Y)$. Prepare a neat, fully labeled sketch of $p_R(r)$,
- (d) Let A denote the event $X^2 \geq Y$. Determine numerical values for the quantities $\mathbf{E}[XY]$ and $\mathbf{E}[XY | A]$.

3. **Example 2.17. Variance of the geometric distribution.** You write a software program over and over, and each time there is probability p that it works correctly, independent of previous attempts. What is the variance of X , the number of tries until the program works correctly?

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