Practice Quiz 1

Name: __________________________________________

Instructions

• DO NOT open this quiz booklet until you are instructed to do so.

• This quiz booklet contains 14 pages, including this one. You have 80 minutes to earn 80 points.

• This quiz is closed book, but you may use one handwritten, double-sided 8 1/2" × 11" crib sheet and the Master Method card handed out in lecture.

• When the quiz begins, please write your name on this coversheet, and write your name on the top of each page, since the pages may be separated for grading.

• Some of the questions are true/false, and some are multiple choice. You need not explain these answers unless you wish to receive partial credit if your answer is wrong. For these kinds of questions, incorrect answers will be penalized, so do not guess unless you are reasonably sure.

• Good luck!

<table>
<thead>
<tr>
<th>Number</th>
<th>Question</th>
<th>Parts</th>
<th>Points</th>
<th>Score</th>
<th>Grader</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>Name on Every Page</td>
<td>14</td>
<td>2</td>
<td></td>
<td></td>
</tr>
<tr>
<td>1</td>
<td>True or False</td>
<td>8</td>
<td>16</td>
<td></td>
<td></td>
</tr>
<tr>
<td>2</td>
<td>Bit Tricks for the Queens Problem</td>
<td>5</td>
<td>13</td>
<td></td>
<td></td>
</tr>
<tr>
<td>3</td>
<td>Parallel PageRank</td>
<td>3</td>
<td>9</td>
<td></td>
<td></td>
</tr>
<tr>
<td>4</td>
<td>Bitonic Sort</td>
<td>6</td>
<td>18</td>
<td></td>
<td></td>
</tr>
<tr>
<td>5</td>
<td>Heap Allocation</td>
<td>3</td>
<td>13</td>
<td></td>
<td></td>
</tr>
<tr>
<td>6</td>
<td>Compilers &amp; Assembly</td>
<td>2</td>
<td>9</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Total</td>
<td></td>
<td></td>
<td>80</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
1 True or False (8 parts, 16 points)

Incorrect answers will be penalized, so do not guess unless you are reasonably sure. You need not justify your answer unless you want to leave open the possibility of receiving partial credit if your answer is wrong.

1.1
Packing is an optimization that reduces data movement but may increase computation.
True  False

1.2
There can never be a true-, anti- or output-data dependence between the following two lines of code:

```
movl %eax, (%esi)
movl (%edi), %ecx
```
True  False

1.3
The `time` command can more readily diagnose kernel-mode performance variations (e.g., page zeroing) than `clock_gettime()`.
True  False

1.4
Using `taskset` for a serial program diminishes performance variations caused by NUMA (nonuniform memory access).
True  False
1.5
When using reference counting for garbage collection, cyclic data structures are never garbage collected.
True  False

1.6
In the free-list heap-allocation algorithm, allocating to the least-full page maximizes the probability that two random accesses hit the same page.
True  False

1.7
Memory-allocator performance is more important when requesting a large amount of memory than when requesting a small amount.
True  False

1.8
Eliminating common subexpressions generally improves the performance of code unless it causes too much register pressure.
True  False
2 Bit Tricks for the Queens Problem (5 parts, 13 points)

Recall the Queens Problem from lecture: Place n queens on an n × n chessboard such that no two
queens can attack each other, i.e., only one queen in placed each row, column, or diagonal:

We saw in lecture that this problem could be solved by a backtracking search that marches up
and down the rows of the chessboard using bit tricks to represent columns and diagonals. In fact,
the problem can be solved by an algorithm even more simple than the one Professor Leiserson
presented in class.

The function queens() performs the backtrack search, returning the number of solutions to the
queens problem. The four arguments to the function are (1) a bit mask mask representing the
width of the board as n columns, (2) a bit mask down representing which columns contain queens,
(3) a bit mask left representing which left-going diagonals ending on the current row contain
queens, and (4) a bit mask right representing which right-going diagonals ending on the current
row contain queens.

The queens() function is called from main() as follows:

```
printf("The %d-queens problem has %d solutions.\n", 
n, 
queens(((1 << n) - 1, 0, 0, 0));
```

The next page shows code for queens() with 5 blanks labeled with letters, as well as a collection
of 20 expressions beneath.
```c
int32_t queens( uint32_t mask,
    uint32_t down,
    uint32_t left,
    uint32_t right ) {
    int32_t count = 0;
    uint32_t possible, place;
    if (down == (A)) return 1;
    for (possible = ~(down|left|right) & mask;
        possible != (B);
        possible &= ~place) {
        place = (C);
        count += queens( mask,
            down|place,
            (D),
            (E));
    }
    return count;
}
```

For each blank in the code, write its label next to the expression that best fits. (*Hint: Some blanks can take more than one expression, but only one is “best.”*)

1. **0**
2. **-1**
3. **down**
4. **left**
5. **left << 1**
6. **(left|place) << 1**
7. **((left|place) << 1) & mask**
8. **mask**
9. **mask + 1**
10. **~mask**
11. **place**
12. **~place**
13. **possible**
14. **possible & (~possible)**
15. **~possible**
16. **right**
17. **right >> 1**
18. **((right|place) >> 1)**
3 Parallel PageRank (3 parts, 9 points)

In the following code, the variables contribution and rank are arrays of doubles, and in_degree and out_degree are arrays of integers. neighbor is a two dimensional array that stores the edges. neighbor[i][j] is the jth neighbor of the ith node.

```c
void pagerank(double * rank, double * contribution, 
              int ** neighbor, int * in_degree, 
              int * out_degree, int num_vertices) {
    for (size_t iter = 0; iter < 10; iter++) {
        cilk_for (size_t i = 0; i < num_vertices; i++) {
            for (int j = 0; j < in_degree[i]; j++) {
                rank[i] += contribution[neighbor[i][j]];
            }
        }
        for (size_t i = 0; i < num_vertices; i++) {
            contribution[i] = rank[i]/out_degree[i];
            rank[i] = 0.0;
        }
    }
}
```

For each of the following code modifications designed to improve performance, circle the appropriate option to specify whether it is safe to make the indicated change, whether it is safe if a reducer is used, or whether it is unsafe. (Note: “safe” means that the output must be exactly the same as for the original code.)

3.1
Replace the for in line 4 with cilk_for.

Safe  Safe with reducer  Unsafe

3.2
Replace the for in line 6 with cilk_for.

Safe  Safe with reducer  Unsafe
3.3
Replace the for in line 10 with cilk_for.

Safe   Safe with reducer   Unsafe
4 Bitonic Sort (6 parts, 18 points)

Consider the following multithreaded implementation of bitonic sort, a sorting algorithm based on bitonic sequences, which are sequences that can be cyclically shifted to be nonincreasing and then nondecreasing. Fortunately, for this problem you must understand neither bitonic sequences nor how the algorithm works. You must only understand its parallelism structure.

```c
// Swap a[i] and a[j] if they are out of order, assuming that
// i < j and the boolean ascending indicates whether the
void bitonic_swap(int *array, size_t i, size_t j, bool ascending) {
    if ((array[i] > array[j]) == ascending) {
        int temp = array[i];
        array[i] = array[j];
        array[j] = temp;
    }
}

// Sort the elements in the subarray a[lo, .., hi-1] into
// ascending/descending order, assuming that the subarray forms
// a bitonic sequence of power-of-2 length.
void bitonic_merge(int *a, size_t lo, size_t hi, bool ascending) {
    if (lo >= hi - 1) return;
    size_t len = (hi - lo) / 2;
    size_t mid = lo + len;
    cilk_for (size_t i = lo; i < mid; i++) {
        bitonic_swap(a, i, i + len, ascending);
    }
    cilk_spawn bitonic_merge(a, lo, mid, ascending);
    bitonic_merge(a, mid, hi, ascending);
    cilk_sync;
}

// Sort the elements in a[lo, .., hi-1] in ascending/descending order
// assuming that the length of the subarray is a power of 2.
void bitonic_sort(int *a, size_t lo, size_t hi, bool ascending) {
    if (lo >= hi - 1) return;
    size_t mid = (hi + lo) / 2;
    cilk_spawn bitonic_sort(a, lo, mid, true);
    bitonic_sort(a, mid, hi, false);
    cilk_sync;
    bitonic_merge(a, lo, hi, ascending);
}
```
For the following questions, let $n = hi - lo$, and assume that $n$ is a power of 2.

4.1
Give a recurrence for the work $M_1(n)$ of bitonic_merge(), solve the recurrence, and express $M_1(n)$ in simple terms.

4.2
Give a recurrence for the span $M_{\infty}(n)$ of bitonic_merge(), solve the recurrence, and express $M_{\infty}(n)$ in simple terms.

4.3
Give the parallelism of bitonic_merge() in simple terms.
4.4

Give a recurrence for the work $S_1(n)$ of bitonic_sort() in terms of $M_1(n)$ and $M_\infty(n)$, solve the recurrence, and express $S_1(n)$ in simple terms.

4.5

Give a recurrence for the span $S_\infty(n)$ of bitonic_sort() in terms of $M_1(n)$ and $M_\infty(n)$, solve the recurrence, and express $S_\infty(n)$ in simple terms.

4.6

Give the parallelism of bitonic_sort() in simple terms.
5 Heap Allocation (3 parts, 13 points)

A certain program needs to allocate memory chunks that have alternating sizes of 60 bytes and 120 bytes. In other words, the program will allocate a chunk of 60 bytes, followed by 120 bytes, followed by 60 bytes, and so on. We shall consider two schemes for heap allocation.

Scheme F is a fixed-size allocator that uses a free-list of 120-byte blocks. Scheme V is a variable-sized allocator that uses binned free lists with blocks that are exact powers of 2.

5.1 What are likely the advantages of Scheme V over Scheme F? (Circle all that apply.)

A Faster allocation.
B Less internal fragmentation.
C Less external fragmentation.
D Fewer TLB (translation lookaside buffer) misses.
E Less false sharing when parallelized.

5.2 Ben Bitdiddle pushes an update to the program. Now, after 100,000 allocations of blocks with alternating sizes of 60 and 120 bytes (as described above), the program frees all blocks of size 60 bytes and proceeds to allocate 100,000 more blocks of size 120 bytes. After the update, which scheme would you prefer to use and why? (Circle all that apply.)

A Scheme V, because freeing blocks is faster with a variable-sized allocator.
B Scheme F, because there is less external fragmentation.
C Scheme F, because there is less internal fragmentation.
D Scheme F, because there is better space utilization and, therefore, fewer TLB (translation lookaside buffer) misses.
E Scheme V, because there is better space utilization and, therefore, fewer TLB (translation lookaside buffer) misses.
5.3

Lem E. Tweakit sends you a mystery Cilk program, in which each allocated object is labeled with the worker thread that created it (its owner), and freed objects are returned to the owner’s heap. What is the bound on blowup $B$ for this mystery Cilk program? (Hint: Blowup is the maximum of allocated storage across all workers divided by the maximum of allocated storage in the serial execution.)

A $B = 1$.

B $B = K$ for some constant $K > 1$.

C $B \leq P$, where $P = \# \text{ workers}$.

D $P < B \leq KP$ for some constant $K > 1$.

E $B > KP$ for any constant $K > 1$. 
6 Compilers & Assembly (2 parts, 9 points)

Consider the four code snippets below. Assume all four examples are compiled with Tapir/Clang on a 64-bit AVX2-enabled Linux machine, using the flags `-Rpass=loop-vectorize -mavx2` (the same conditions you used to complete Homework 3).

**A**

```c
void func_A(int32_t * restrict X, int32_t * restrict Y) {
    for (int i = 0; i < 1000*1000; i++) {
        X[i] = X[i] + Y[i];
    }
}
```

**B**

```c
void func_B(int32_t * restrict X, int32_t * restrict Y) {
    for (int i = 0; i < 1000*1000; i+=4) {
        X[i] = X[i] + Y[i];
    }
}
```

**C**

```c
void func_C(int32_t * restrict X, int32_t * restrict Y) {
    for (int i = 0; i < 1000*1000; i++) {
        X[i] = X[i] / Y[i];
    }
}
```

**D**

```c
void func_D(int32_t * restrict X, int32_t * restrict Y) {
    for (int i = 0; i < 1000*1000 - 1; i++) {
        X[i] = X[i+1] + Y[i];
    }
}
```
6.172 Practice Quiz 1

Name ________________________________ 14

6.1

For which of the functions is the loop likely to be vectorized without further compiler directives? (Circle all that apply.)

A func_A
B func_B
C func_C
D func_D

6.2

The following text is the assembly code for one of the loops:

```
movq %rdi, -8(%rbp)  # X
movq %rsi, -16(%rbp)  # Y
movl $0, -20(%rbp)
.LBB0_1:
cmpl $1000000, -20(%rbp)
jge .LBB0_4
movslq -20(%rbp), %rax
movq -8(%rbp), %rcx
movl (%rcx,%rax,4), %edx
movslq -20(%rbp), %rax
movq -16(%rbp), %rcx
addl (%rcx,%rax,4), %edx
movslq -20(%rbp), %rax
movq -8(%rbp), %rcx
movl %edx, (%rcx,%rax,4)
movl -20(%rbp), %eax
addl $4, %eax
movl %eax, -20(%rbp)
jmp .LBB0_1
.LBB0_4:
```

Circle the letter for the function containing the loop corresponding to the assembly code.

A func_A
B func_B
C func_C
D func_D
### Intel x86 Assembly Language Cheat Sheet

<table>
<thead>
<tr>
<th>Instruction</th>
<th>Effect</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Data movement</strong></td>
<td></td>
</tr>
<tr>
<td>mov src, dest</td>
<td>Copy src to dest</td>
</tr>
<tr>
<td>mov $10, %eax</td>
<td></td>
</tr>
<tr>
<td><strong>Arithmetic</strong></td>
<td></td>
</tr>
<tr>
<td>add src, dest</td>
<td>Dest = dest + src</td>
</tr>
<tr>
<td>add $10, %esi</td>
<td></td>
</tr>
<tr>
<td>mul reg</td>
<td>edx:eax = eax * reg (colon means the result spans across two registers)</td>
</tr>
<tr>
<td>mul %esi</td>
<td></td>
</tr>
<tr>
<td>div reg</td>
<td>edx = edx:eax mod reg</td>
</tr>
<tr>
<td>div %edi</td>
<td></td>
</tr>
<tr>
<td>inc dest</td>
<td>Increment destination</td>
</tr>
<tr>
<td>Inc %eax</td>
<td></td>
</tr>
<tr>
<td>dec dest</td>
<td>Decrement destination</td>
</tr>
<tr>
<td>dec (%esi)</td>
<td></td>
</tr>
<tr>
<td>sbb arg1, arg2</td>
<td>if CF = 1, (this is set by cmp instruction; refer cmp)</td>
</tr>
<tr>
<td>sbb %eax, %ebx</td>
<td></td>
</tr>
<tr>
<td>else</td>
<td>arg2 = arg2 – (arg1 + 1)</td>
</tr>
<tr>
<td>else</td>
<td>arg2 = arg2 – arg1</td>
</tr>
</tbody>
</table>

**Function Calls**

<table>
<thead>
<tr>
<th>Instruction</th>
<th>Effect</th>
</tr>
</thead>
<tbody>
<tr>
<td>call label</td>
<td>Push eip, transfer control</td>
</tr>
<tr>
<td>call _fib</td>
<td></td>
</tr>
<tr>
<td>ret</td>
<td>Pop eip and return</td>
</tr>
<tr>
<td>ret</td>
<td></td>
</tr>
<tr>
<td>push item</td>
<td>Push item (constant or register) to stack</td>
</tr>
<tr>
<td>pushl $32</td>
<td></td>
</tr>
<tr>
<td>pushl %eax</td>
<td></td>
</tr>
<tr>
<td>pop [reg]</td>
<td>Pop item from stack; optionally store to register</td>
</tr>
<tr>
<td>pop %eax</td>
<td></td>
</tr>
<tr>
<td>popl</td>
<td></td>
</tr>
</tbody>
</table>

**Bitwise Operations**

<table>
<thead>
<tr>
<th>Instruction</th>
<th>Effect</th>
</tr>
</thead>
<tbody>
<tr>
<td>and src, dest</td>
<td>Dest = src &amp; dest</td>
</tr>
<tr>
<td>and %ebx, %eax</td>
<td></td>
</tr>
<tr>
<td>or src, dest</td>
<td>Dest = src</td>
</tr>
<tr>
<td>orl (0x2000), %eax</td>
<td></td>
</tr>
<tr>
<td>xor src, dest</td>
<td>Dest = src ^ dest</td>
</tr>
<tr>
<td>xor $0xffffffff, %eax</td>
<td></td>
</tr>
<tr>
<td>shi count, dest</td>
<td>Dest = dest &lt;&lt; count</td>
</tr>
<tr>
<td>shi $2, %eax</td>
<td></td>
</tr>
<tr>
<td>shr count, dest</td>
<td>Dest = dest &gt;&gt; count</td>
</tr>
<tr>
<td>shr $4, (%eax)</td>
<td></td>
</tr>
<tr>
<td>sai count, dest</td>
<td>Same as shi, shifted bits will be the sign bit</td>
</tr>
</tbody>
</table>

**Conditionals and jumps**

<table>
<thead>
<tr>
<th>Instruction</th>
<th>Effect</th>
</tr>
</thead>
<tbody>
<tr>
<td>cmp arg1, arg2</td>
<td>If arg1 &gt; arg2 sets CF=1 (carry flag =1)</td>
</tr>
<tr>
<td>This compares arg1 and arg2; you can use any conditionals jumps below to act upon the result of this comparison</td>
<td></td>
</tr>
<tr>
<td>cmp $0, %eax</td>
<td></td>
</tr>
<tr>
<td>test reg, imm/reg</td>
<td>Bitwise and of register and constant/register; the next jump command uses the result of this; consider this essentially as same as compare</td>
</tr>
<tr>
<td>test %rax, %rcx</td>
<td></td>
</tr>
<tr>
<td>je label</td>
<td>Jump to label if arg2 = arg1</td>
</tr>
<tr>
<td>je endloop</td>
<td></td>
</tr>
<tr>
<td>jne label</td>
<td>Jump to label if arg2 != arg1</td>
</tr>
<tr>
<td>jne loopstart</td>
<td></td>
</tr>
<tr>
<td>jg / ja label</td>
<td>Jump to label if arg2 &gt; arg1</td>
</tr>
<tr>
<td>jg exit / ja exit</td>
<td></td>
</tr>
<tr>
<td>jge label</td>
<td>Jump to label if arg2 &gt;= arg1</td>
</tr>
<tr>
<td>jge format_disk</td>
<td></td>
</tr>
<tr>
<td>jl label</td>
<td>Jump to label if arg2 &lt; arg1</td>
</tr>
<tr>
<td>jl error</td>
<td></td>
</tr>
<tr>
<td>je label</td>
<td>Jump to label if arg2 &lt;= arg1</td>
</tr>
<tr>
<td>je finish</td>
<td></td>
</tr>
<tr>
<td>jz label</td>
<td>Jump to label if bits were not set</td>
</tr>
<tr>
<td>jz looparound</td>
<td></td>
</tr>
<tr>
<td>jnz label</td>
<td>Jump to label if bits were set</td>
</tr>
<tr>
<td>jnz error</td>
<td></td>
</tr>
<tr>
<td>jump label</td>
<td>Unconditional jump</td>
</tr>
<tr>
<td>jmp exit</td>
<td></td>
</tr>
</tbody>
</table>

**Miscellaneous**

<table>
<thead>
<tr>
<th>Instruction</th>
<th>Effect</th>
</tr>
</thead>
<tbody>
<tr>
<td>nop</td>
<td>No-op</td>
</tr>
<tr>
<td>nop</td>
<td></td>
</tr>
<tr>
<td>lea addr, dest</td>
<td>Move the address calculated to the dest</td>
</tr>
<tr>
<td>lea 23(%eax, %ecx,8),%eax</td>
<td></td>
</tr>
<tr>
<td>cqto</td>
<td>%rdx:%rax— sign-extend of %rax.</td>
</tr>
<tr>
<td>cqto</td>
<td></td>
</tr>
</tbody>
</table>

**Suffixes**
- b=byte(8)
- w=word(16)
- l=long(32)
- q=quad(64)

**Base Indexed Scale Displacement**
- $172(%rdi, %rdx,8) = %rdi + 8 * %rdx + 172$

Note that not both src and dest can be memory operands at the same time.
- register - %eax
- fixed address – (0x1000)
- constant - $10
- dynamic address – (%rsi)