mas.s62
lecture 17
coinjoin, signature aggregation
2018-04-11
Tadge Dryja

## today

privacy
coinjoin
aggregate signatures
schnorr multi-signatures
aggregation and attacks

## privacy

related terms: anonymity, fungibility whatever the term, I don't need any. I've got nothing to hide.

## privacy

if you don't have anything to hide, you don't have any bitcoin literally; the instant your private key is publicly known, someone will take your bitcoins

## fungibility

often used as a euphemism for privacy / anonymity
means every bitcoin is "the same" important for things that strive to be money
gold is fungible, diamonds are not

## fungibility

currency legally considered fungible
Crawfurd v The Royal Bank (1749)
guy writes his name on a £20 note, loses it. The note shows up later at the bank, he demands it back. Court says nope, that's not how money works.

## fungibility

bitcoin does not enjoy the same legal protections; not considered currency by most govts
so it's up to the software to enforce fungibility of the coins
real world case
customer buys coins
customer transfers coins to UK betting shop. bets on game \& wins customer transfers winnings back to US exchange to sell. exchange closes the account as violation of ToS problem. . .?
real world case
those coins are "worth less" than other coins, because of where they're from
very un-money-like!
if we want to make bitcoin money, how to fix this?

## address re-use

simplest loss of privacy
persistent use of a pubkey web explorers treat addresses as having balances

## guessing change outputs

tx with 1 in, 2 out
input: 10 coins
output a: 1 coin
output b: 8.9997 coin
guess which goes to the same person

## anonymity set

terms: anonymous, pseudonymous anonymity set
even if $I$ can't trace the bitcoins, I know it belongs to someone who has bitcoins! Which most people don't. try to increase anonymity set

## how to lose the trail

 bitcoin mixers!coins at address A
send 10 coins to the mixer, addr $B$
later, 4 coins to addr C
later, 6 coins to addr D

## mixers

mixers work well
potential anonymity set is all other users of mixer
problem: mixers disappear with everyone's money. consistently.

## coinjoin

I taint rich (maxwell,
bitcointalk.org, 2013)
mixing multiple users within a single transaction

## coinjoin tx

two different people in the same tx

| input 0 <br> user A signature <br> 10 coins | output 0 <br> address C <br> 2 coins |
| :--- | :--- |
| input 1 <br> user B signature <br> 2 coins | output 1 <br> address D <br> 10 coins |

## coinjoin tx

fun first (2nd?) tx
69d9d66aae4812b6cf156f32267b773fb2118db696bb847ebd3454a198b59fbd

| input 0 <br> user A signature <br> 10 coins | output 0 <br> address C <br> 2 coins |
| :--- | :--- |
| input 1 <br> user B signature <br> 2 coins | output 1 <br> address D <br> 10 coins |

## coinjoin tx

## problems with this model?

 any way to tell who's who?| input 0 <br> user A signature <br> 10 coins | output 0 <br> address C <br> 2 coins |
| :--- | :--- |
| input 1 <br> user B signature <br> 2 coins | output 1 <br> address D <br> 10 coins |

## coinjoin tx

 gee, maybe $A->D, B->C$
## amounts are different

$\left.$| input 0 |
| :--- | :--- |
| user A signature |
| 10 coins |$\quad$| output 0 |
| :--- |
| address C |
| 2 coins | \right\rvert\, | input 1 |
| :--- | :--- |
| user B signature |
| 2 coins |$\quad$| address D |
| :--- |
| 10 coins |

## coinjoin tx how about this?

| A signature 10 coins | address C 1 coin |
| :--- | :--- |
| B signature 2 coins | address D 7 coins |
|  | address E 1 coin |
|  | address F 3 coins |

## coinjoin tx how about this?

... nice try but still no

| A signature 10 coins | address C 1 coin |
| :--- | :--- |
| B signature 2 coins | address D 7 coins |
|  | address E 1 coin |
|  | address F 3 coins |

## coinjoin tx

## now?

| A signature 10 coins | address C 2 coins |
| :--- | :--- |
| B signature 2 coins | address D 2 coins |
|  | address E 8 coins |
|  |  |

## coinjoin tx

 this actually works; unclear if output C is from user A or B| A signature 10 coins | address C 2 coins |
| :--- | :--- |
| B signature 2 coins | address D 2 coins |
|  | address E 8 coins |
|  |  |

## improving on coinjoin

have more users, bigger anonymity set problem: users themselves know the mapping of inputs to outputs, can leak this info, hurtning anonymity

## improving on coinjoin

 coinshuffle: pre-coinjoin messaging to shuffle inputs and outputsif at least 2 participants are honest, mapping is private

## coinshuffle

everyone make public keys, send to everyone else. everyone also broadcast inputs
encrypt your output with everyone's pubkeys sequentially
enc $_{c}\left(\right.$ enc $_{b}\left(\right.$ enc $_{a}($ output $\left.\left.)\right)\right) \rightarrow$ hand to a

## coinshuffle

user a receives encrypted outputs, shuffles and decrypts
hands still encrypted outputs to next user, who decrypts, shuffles
final user gets the outputs, but can't tell which belong to whom everyone signs this tx
real world issues some people use this!
... which people use this?
limited anonymity set of people who really want anonymity.
which is not the anonymity set the people who want anonymity want.

## make coinjoin cheaper

 people don't care about privacy other people's privacy = externalityeveryone likes cheaper txs though

# make coinjoin cheaper 

 privacy and scalability can work togetherless information to store, less information to link to users

## aggregate signatures current signatures

$\left.$| input 0 |
| :--- | :--- |
| user A signature |
| 10 coins |$\quad$| output 0 |
| :--- |
| address E |
| 2 coins | \right\rvert\, | input 1 |
| :--- | :--- |
| user B signature |
| 2 coins |$\quad$| address F |
| :--- |
| 10 coins |

## aggregate signatures aggregate signatures

| input 0 | output 0 <br> address E <br> 2 coins |
| :--- | :--- |
| 10 coins | output 1 <br> input 1 <br> 2 address $F$ <br> 10 coins signature |

## aggregate signatures

how to make this signature?
Given
pubkeys A, B
message m
need one signature $R$, s

## aggregate signatures

signature equation
$s=k-h(m, R) c$
$s G=R-h(m, R) C$
make $c=a+b$, but need to not share private keys

## aggregate signatures

first, share $R$
alice: make $k_{a}$, compute $R_{a}$, share $R_{a}$
bob: make $k_{b}$, compute $R_{b}$, share $R_{b}$

## aggregate signatures

## next, add R

both: compute $R=R_{a}+R_{b}$

## aggregate signatures

next, compute s's
alice: $s_{a}=k_{a}-h(m, R) a$
bob: $s_{b}=k_{b}-h(m, R) b$
share $\mathrm{S}_{\mathrm{a}}$ and $\mathrm{S}_{\mathrm{b}}$

## aggregate signatures

finally, compute s sum
$\mathrm{s}=\mathrm{s}_{\mathrm{a}}+\mathrm{s}_{\mathrm{b}}$
$=k_{a}+k_{b}-h(m, R) a-h(m, R) b$
$=k-h(m, R)(a+b)$
$s G=R-h(m, R) C$
works!

## aggregate signatures

now users can save space, only 1 signature for $n$ inputs

| input 0 | output 0 <br> address E <br> 2 coins |
| :--- | :--- |
| 10 coins | output 1 <br> input 1 <br> C signature <br> 2 coins |
| 10 coins |  |

## key attacks

 problem: wait, I didn't sign that...| input 0 | output 0 <br> address E <br> 40002 coins |
| :--- | :--- |
| input 1 <br> user A\&B signature <br> 2 coins |  |

rogue key attacks
observe (rich) key A on network make q , compute $\mathrm{qG}=\mathrm{Q}$
compute $\mathrm{B}=\mathrm{Q}-\mathrm{A}$
send some coins to key B
note that you don't know b, and can't sign
rogue key attacks spend from B and A
you don't know b, you don't know a even though you don't know the private key for either, you know the private key for both!
$c=a+b=a+(q-a)=q$
rogue key attacks
require proof of knowledge of b make b sign a message before combining keys
rogue key attacks require proof of knowledge of b make b sign a message before combining keys
... but the whole point was to aggregate signatures!

## delinearization

redefine signatures - still send to C instead of singing with $C=A+B$, sign with $C=(A * h(A))+(B * h(B))$

## delinearization

sign with $C=A * h(A)+B * h(B)$
$c=a * h(A)+b * h(B)$
I know $b=q-a, I$ know $q$
$c=a * h(A)+(q-a) * h(Q-A)$

## delinearization

sign with $C=A * h(A)+B * h(B)$
$c=a * h(A)+b * h(B)$
I know $b=q-a, I$ know $q$
$c=a * h(A)+(q-a) * h(Q-A)$
can't get rid of $a * h(A)$ term

## Wagner's birthday

 this actually isn't enough!Wagner: A Generalized Birthday Problem
Finding a collision is hard, right?
$2^{\text {n/2 }}$ time
but that's a 2-collision

Wagner's birthday
2 collision: find A, B s.t. A = B general collision
find $A_{0}, A_{1} \ldots A_{1}, B_{0}, B_{1} \ldots B_{j}$ s.t.
$\Sigma \mathrm{A}=\Sigma \mathrm{B}$
if you have lots of As and Bs, gets easier
improved delinearization take the hash of all the keys together $z=h(A, B)$
sign with $C=A * h(z, 0)+B * h(z, 1)$
$c=a * h(z, 0)+b * h(z, 1)$
this works, paper calls it "MuSig"

## aggregate signatures

first use: within my own wallet

## saves space

| input 0 (mine) | output 0 <br> address E <br> 4 coins |
| :--- | :--- |
| input 1 (mine) <br> 3 signature | output 1 <br> address F <br> 1 coin |

## aggregate signatures <br> cooler use: with coinjoin

| A 3 coins | address E 3 coin |
| :--- | :--- |
| B 3 coins | address F 3 coins |
| C 3 coins | address G 3 coin |
| D 3 coins signature | address H 3 coins |

## aggregate signatures

helps scalability and privacy
coinjoin tx is cheaper than solo tx one giant tx per block, with 1 sig? what about amounts... still an issue (next time: how to mix amounts)

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MAS.S62 Cryptocurrency Engineering and Design
Spring 2018

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