Problems: Chain Rule Practice

One application of the chain rule is to problems in which you are given a function of $x$ and $y$ with inputs in polar coordinates. For example, let $w = (x^2 + y^2)xy$, $x = r \cos \theta$ and $y = r \sin \theta$.

1. Use the chain rule to find $\frac{\partial w}{\partial r}$.

2. Find the total differential $dw$ in terms of $dr$ and $d\theta$.

3. Find $\frac{\partial w}{\partial r}$ at the point $(r, \theta) = (2, \pi/4)$. 