

Studio 5: Bayesian Updating

18.05 Spring 2014

You should have downloaded studio5.zip and unzipped it into your 18.05 working directory.

Board question

1. Consider the random die problem: 5 dice with sides 4, 6, 8, 12 or 20. I choose one die at random and roll it repeatedly, reporting the results to you. Your job is to figure out which die I chose.

(a) List all possible hypotheses.

(b) List all possible outcomes for the j th roll.

(c) Let x_j be the random variable equal to the outcome of the j th roll, $j = 1, 2, \dots$

Write out the entire likelihood table for the j th roll. The table has a column of likelihoods for each possible outcome.

R question

2. (a) Go through the simulation of Bayesian updating in studio5.r. After running through the loop of 20 rolls be sure to click through all the plots in RStudio.

(b) Use the same `dataRolls` as in part (a) and redo the simulation with a new prior distribution.

\mathcal{H}	4	6	8	12	20
$P(\mathcal{H})$.05	.05	.05	.05	.80

(c) Describe how the posterior distributions compare.

(d) Redo the simulation with the original prior distribution but generate the sample rolls `dataRolls` from a 20-sided die.

Censored data

3. Suppose we only observe **censored** values of the rolls. For the j th roll we observe

$$y_j = \begin{cases} 1 & \text{if } x_j = 1 \\ 0 & \text{if } x_j \neq 1 \end{cases}$$

Instead of the actual rolls you only see the censored data y_1, y_2, \dots

- (a) List all the possible hypotheses.
- (b) Write out the entire likelihood table for one roll y_j .
- (c) Modify the R simulation to simulate this censored scenario.
- Use `nrolls = 20` in the simulation. After the 20th roll has the posterior nearly converged on the true hypothesis?
 - Investigate how many rolls are needed to see a clear convergence of the posterior distribution.

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18.05 Introduction to Probability and Statistics

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