Consider a single proton exchange membrane fuel cell operated at 80°C with pure H₂ and pure O₂ inputs at 150 kPa, in which Pt nanoparticles supported on carbon are used as the electrocatalyst for hydrogen oxidation and oxygen reduction. The anode and cathode electrode areas are 5 cm². The ohmic resistance across the fuel cell is $5 \cdot 10^{-3}$ ohms. The exchange current densities for the rate determining steps of oxygen reduction and hydrogen oxidation on Pt nanoparticles are $5 \times 10^{-11}$ A/cm² and $1 \times 10^{-3}$ A/cm², respectively.

1) Calculate the equilibrium fuel cell voltage under the operating conditions.
2) Develop an analytical expression that relates the fuel cell operating voltage to the current density obtainable from the fuel cells by considering ohmic and activation overpotentials across the cell. Plot the effect of ohmic and activation overpotentials to the fuel cell voltage loss as a function of current density in mA/cm² in the range from 0 to 2 A/cm².
3) Plot the second law efficiency of the fuel cell (see equation 2.7 in lecture note on electrochemical thermodynamics (electrochemLecturenote1.pdf)) and the power density in W/cm² as a function of current density in mA/cm².

Please state all assumptions clearly.