$$\sigma(-x) = 1 - \sigma(x)$$

$$\frac{d\sigma}{dx} = \sigma\left(1 - \sigma\right)$$