This is a 3 part question dealing with the wind-driven circulation. At
26°N in the N. Atlantic, the average wind stress across the interior of
the basin from the eastern boundary to the Bahamas is: \((\tau^x, \tau^y) = (-.034, -.01) \text{ Nt/m}^2\). The average vertical component of the wind
stress curl across this latitude is estimated to be \(-7.26 \times 10^{-8} \text{ Nt/m}^3\).
The values have come from a climatology for the period 1991-1997
developed by NCEP. Using these values, 1) estimate the values of
the total (zonally integrated) meridional Ekman and Sverdrup
transports at this latitude. The Florida Current flows through the
Florida Straits to the west of the Bahamas. 2) What transport would
one expect to observe if the Sverdrup balance was perfect for the
interior? What is observed? If one were interested in estimating the
meridional \textit{geostrophic} transport in the interior across this latitude
using only hydrography, 3) how might one use the above information
to estimate a “reference level” for the geostrophic calculation using
density or dynamic height?
12.808, Problem 2, problem set #2

In this problem you are asked to use MATLAB to analyze real data from the Gulf Stream. Six CTD stations were collected crossing the Gulf Stream 2003 [& so TJ missed some 12.808 lectures]. In addition, a lowered ADCP (LADCP) measured horizontal currents at each station. These files can be found in the assignment page. You are asked to:

1. Plot the temperature/salinity data from the 6 stations in a T/S diagram & briefly discuss where there are large differences among the stations (see right for example of a T/S diagram for sta. 67)

2. Calculate the geostrophic velocity for the water column for each station pair assuming a level of no motion at 2000 dbar.
3. Consider how to use the LADCP measurements to adjust the assumed level of no motion at 2000 dbar (e.g. one could take the mean of each station pair and use it to shift the geostrophic velocity at 2000 dbar). This was done at the right yet the two don’t agree everywhere.

4. Extra Credit! Use the result from 3) to estimate the total geostrophic volume transport in the upper 4000m for the 6 stations.

This problem requires some familiarity with MATLAB. Please read the README file for problem set #2 for guidance. Remember, that to compare geostrophic with measured velocities, one has to look at velocity normal to the line between each station pair! [Hint: use “sw_dist.m” to get bearing between station pairs.]
This problem is for PO students: it is optional for others. Using the barotropic momentum and continuity equations for a variable depth ocean of constant density presented in the class notes, derive the conservation statement (below) for potential vorticity in the presences of body forces and friction for a spatially variable Coriolis parameter. Recall that this was stated as a result in class: you are now asked to show how this equation can be obtained. Recall that $D=H+h$, where $z = -H$ is the depth of the undisturbed fluid and $z = h$ is the free surface.

$$
\frac{d}{dt} \left[ \frac{f + \zeta^z}{D} \right] = -\frac{r}{D} \zeta + \frac{1}{\rho D} (F_x^y - F_y^x) = -\frac{r}{D} \zeta + \frac{1}{\rho D} (\nabla_h \times \vec{F})
$$