**Instructions:** Please solve the following exercises using MATLAB. One simple way to present your solutions is to copy all of your code and results (plots, numerical answers, etc.) into a Word document, which you should submit in class. There is no online submission. **Do NOT share code!**

**Exercise 1 (30 pts)**
To determine whether glaucoma affects the corneal thickness, measurements were made in 8 people affected by glaucoma in one eye but not in the other. The corneal thicknesses (in microns) were as follows:

<table>
<thead>
<tr>
<th>Person</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
<th>7</th>
<th>8</th>
</tr>
</thead>
<tbody>
<tr>
<td>Eye affected by glaucoma</td>
<td>488</td>
<td>478</td>
<td>480</td>
<td>426</td>
<td>440</td>
<td>410</td>
<td>458</td>
<td>460</td>
</tr>
<tr>
<td>Eye not affected by glaucoma</td>
<td>484</td>
<td>478</td>
<td>492</td>
<td>444</td>
<td>436</td>
<td>398</td>
<td>464</td>
<td>476</td>
</tr>
</tbody>
</table>

Assume the corneal thicknesses are normally distributed with mean $\mu_1$ and variance $\sigma_1^2$ for eyes affected by glaucoma, and mean $\mu_2$ and variance $\sigma_2^2$ for eyes not affected by glaucoma. Test $H_0: \mu_1 = \mu_2$ against $H_1: \mu_1 < \mu_2$ using $\alpha = 0.1$. What kind of test will you perform? Base your conclusion on a 90% confidence interval.

**Solution**

Here is the script and the results:

```matlab
clear all;
clc;

alpha = 0.1;
x = [488 478 480 426 440 410 458 460];
y = [484 478 492 444 436 398 464 476];

[h,p,ci,stats] = ttest(x,y,alpha,'left')
```

```plaintext
h = 0

p = 0.1637

ci = -Inf 1.3746
```
The upper 90% CI is \((-\infty, 1.3746]\), which includes 0, so we do not reject \(H_0\).

Exercise 2 (70 pts)
The following data give the barometric pressure \(x\) (in inches of mercury) and the boiling point \(y\) (in °F) of water in the Alps.

\[
\begin{array}{ccc}
\hline
x & y & x & y & x & y \\
20.79 & 194.5 & 23.89 & 200.9 & 28.49 & 209.5 \\
20.79 & 194.3 & 23.99 & 201.1 & 27.76 & 208.6 \\
22.40 & 197.9 & 24.02 & 201.4 & 29.04 & 210.7 \\
22.67 & 198.4 & 24.01 & 201.3 & 29.88 & 211.9 \\
23.15 & 199.4 & 25.14 & 203.6 & 30.06 & 212.2 \\
23.35 & 199.9 & 26.57 & 204.6 & & \\
\hline
\end{array}
\]

a. Make a scatterplot with pressure \(x\) on the \(x\)-axis and boiling point \(y\) on the \(y\)-axis. Does the relationship appear to be approximately linear?
b. Fit a least-squares line. What are the coefficients of the line? What are their t-statistics?
c. Plot the least-squares line in the same figure with the scatterplot.
d. What proportion of variation in the boiling point is explained by the linear regression model on the barometric pressure?
e. Is the slope coefficient significantly different from zero? How do you know? If yes, at what significance level?
f. What are SSR, SSE, SST, MSR, MSE and F?

Solution

Here is the script and the results:

```matlab
a,c.
clear all;
clc;
close all;

boiling_point = [194.5, 194.3, 197.9, 198.4, 199.4, 199.9, 200.9, 201.1, 201.4, 201.3, 203.6, 204.6, 209.5, 208.6, 210.7, 211.9, 212.2];

% Scatterplot
plot(pressure, boiling_point,'x');
grid;
```
Yes, the relationship appears approximately linear.

b.
% Run the regression
whichstats = {'beta','r', 'mse', 'rsquare', 'tstat', 'fstat'};
stats = regstats(boiling_point, pressure,'linear',whichstats);

betas = stats.beta
tstats = stats.tstat.t
pvals = stats.tstat.pval
rsquare = stats.rsquare

betas = 

155.2965
1.9018

tstats =

167.4650
51.7408

pvals =

1.0e-017 *
The coefficients of the line are $\hat{\beta}_0 = 155.2965$ and $\hat{\beta}_1 = 1.9018$.

d. The proportion of variation in boiling point explained by the model is $r^2 = 0.9944$.

e. Yes, $\hat{\beta}_1$ is significantly different from zero. The p-value is nearly zero ($<2e-16$), so the difference is significant for any reasonable $\alpha$.

f.

Regression ANOVA

<table>
<thead>
<tr>
<th>Source</th>
<th>df</th>
<th>SS</th>
<th>MS</th>
<th>F</th>
<th>P</th>
</tr>
</thead>
<tbody>
<tr>
<td>Regr</td>
<td>1.0000</td>
<td>527.8249</td>
<td>527.8249</td>
<td>2677.1053</td>
<td>0.0000</td>
</tr>
<tr>
<td>Resid</td>
<td>15.0000</td>
<td>2.9574</td>
<td>0.1972</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Total</td>
<td>16.0000</td>
<td>530.7824</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>