NAME: ____________________________

COURSE 3.00: THERMODYNAMICS OF MATERIALS

90 minute EXAM, Oct 12, 2001

PROBLEM 1 (20 POINTS)____________

PROBLEM 2 (20 POINTS)____________

PROBLEM 3 (20 POINTS)____________

PROBLEM 4 (20 POINTS)____________

PROBLEM 5 (20 POINTS)____________

TOTAL (100 POINTS) ____________

You can either write your answer on the question sheets or use separate pages. In each case make sure your answer is clearly marked.

*A neat answer is the sign of a clear mind*
Question 1

I have a machine stirring in a bucket with liquid. The bucket is under constant pressure and is insulated from the environment (an adiabatic bucket).

Check of the correct answer.

a) Which of the following statements regarding the enthalpy of the bucket during this process is correct? The bucket is defined as the physical bucket + the liquid in it.

\[ \Delta H_{\text{bucket}} > 0 \] \[ \Delta H_{\text{bucket}} < 0 \] \[ \Delta H_{\text{bucket}} = 0 \]

b) Which of the following statements regarding the entropy of the bucket during this process is correct? The bucket is defined as the physical bucket + the liquid in it.

\[ \Delta S_{\text{bucket}} > 0 \] \[ \Delta S_{\text{bucket}} < 0 \] \[ \Delta S_{\text{bucket}} = 0 \]

c) Which of the following statements regarding the enthalpy of the surroundings is correct?

\[ \Delta H_{\text{surr}} > 0 \] \[ \Delta H_{\text{surr}} < 0 \] \[ \Delta H_{\text{surr}} = 0 \]

d) What is the minimal entropy change that needs to place in the surroundings? 

\[ \Delta S_{\text{surr}} > 0 \] \[ \Delta S_{\text{surr}} < 0 \] \[ \Delta S_{\text{surr}} = 0 \]
Question 2

A super-elastic single crystal can transform between two phases (α and β) which have different unit cells, and hence different shape. At room temperature (298K) a super-elastic strain of 7% can be achieved at a uniaxial stress of 30MPa.

a) Define the relevant thermodynamic potential which is minimal under conditions of constant applied force and constant temperature. Write the differential of this potential. You can neglect the work performed by/on the atmospheric pressure.

b) For its application, the stress needed to achieve the super-elastic strain can not exceed 100MPa or be below 10MPa. Calculate the temperature range in which the material can operate. Clearly state the assumptions made as you derive your result!

DATA:
enthalpy for the transformation from α to β: ΔH = 300J/mol
molar volume: V ≈ 8 cm³/mol

Please show necessary derivation
Question 3:

Two systems, each containing chemical species A, B, and C in different concentrations, are in contact through a semi-permeable wall. The semi-permeable wall does not allow for transport of A, B, or C individually, but only allows a pair of molecules A-B to pass through together. The systems can be considered to be at constant temperature and pressure.

Derive the equilibrium conditions imposed on the chemical potentials for this system.
Question 4:

In class we derived an expression for $dS$ in terms of $dP$ and $dT$. Derive two other expressions for $dS$: one in terms of $dT$, $dV$, another in terms of $dV$, $dP$. Write the expressions in terms of heat capacities, compressibilities and coefficients of thermal expansion. Use the symbol $\alpha$ for thermal expansion, $\beta$ for compressibility, and $C$ for heat capacity. If further specification of the property is necessary, please use indices (e.g. $C_p$ is constant pressure heat capacity etc.).
Problem 5:

A system has the equation of state $H = A T$, where $A = 100 \text{J/K}$. Assume this equation of state is valid in the temperature range from 1K to 500K. The system is cooled from 298K to 1K by operating a refrigerator with the high temperature heat release at 298K. The low temperature heat absorption cools the system.

What is the minimum work required to cool this system from 298 K to 1K?